

*Uncertainty Evaluation of Nuclear Reaction Model
Parameters using Integral and Microscopic Measurements
Covariances Evaluation with CONRAD Code*

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Conrad

Functionalities

- Evaluation : analysis of microscopic, semi-integral and integral measurements,
- Bayesian parameters estimations (GLS),
- Uncertainty propagation and evaluation with Monte-Carlo or Analytical methods
- establish a link with reactor physicists : from $\sigma(E)$ to σ_g

Nuclear reactions models in Conrad

- Resolved resonance range (MLBW, Reich-Moore,...),
- Unresolved resonance range (average R matrix)
- Statistical models (Hauser-Feshbach, Moldauer, GOE,...)
- Continuum (ECIS and TALYS wrapper)

From 0eV to 20MeV : all models in the same framework



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Goals of Covariances Estimations :

- understanding of experiments

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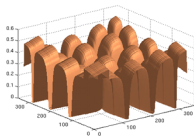
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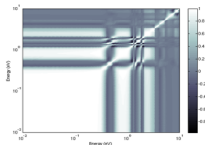
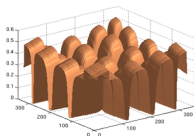
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Goals of Covariances Estimations :

- understanding of experiments
- knowledge of nuclear reaction models and cross sections
- feed Evaluated Nuclear Data Files (ENDF,JEFF,...)





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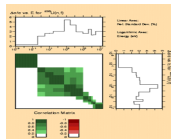
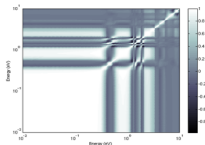
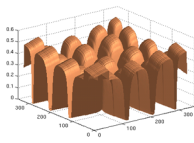
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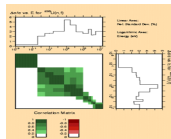
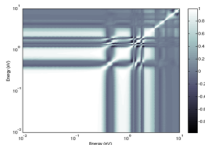
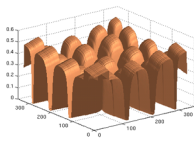
Goals of Covariances Estimations :

- understanding of experiments
- knowledge of nuclear reaction models and cross sections
- feed Evaluated Nuclear Data Files (ENDF,JEFF,...)
- inputs for applications (reactor physics, fusion, protection, etc ...)



Goals of Covariances Estimations :

- understanding of experiments
- knowledge of nuclear reaction models and cross sections
- feed Evaluated Nuclear Data Files (ENDF,JEFF,...)
- inputs for applications (reactor physics, fusion, protection, etc ...)
- focusing on nuclear reaction model parameters or cross sections



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Recurrent puzzle :

- take into account **ALL** uncertainties (including experimental ones) and propagate to
 - nuclear reaction model parameters
 - or cross sections ...
- mass production techniques developed for adding uncertainty information in Evaluated Nuclear Data Files
- low fidelity covariances,
- Major drawbacks found by reactor physicists
 - most of the time the integral experiments were not taken into account sufficiently soon in the evaluation process,
 - unexpected discrepancies,
 - "Are you sure of these covariances ?"



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Model Parameter Definition

Between $[0\text{eV}; 20\text{MeV}]$:

Phenomenological cross section are based on nuclear reaction models with parameters not always predicted by theory.

Model parameters : referred as \vec{x} in this presentation

- Resolved Resonance Range : $E_\lambda, \gamma_\lambda^i, R_{\text{eff}}, \dots$,
 - Unresolved Resonance Range : $D_0, \langle \Gamma^i \rangle, R_{\text{eff}}, \dots$,
 - Higher energies : Optical model parameters
-
- parameters used to calculate cross sections covariances.
 - Data assimilation technique to estimate the parameters : use of Experiments
 - thus \Rightarrow experimental parameters (with uncertainties)

How to clearly distinguish the model and "nuisance" parameters in the uncertainty propagation procedure ?



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Nuisance Parameter Definition



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Nuisance parameters : referred as $\vec{\theta}$ in this presentation

- Experimental parameters : sample composition, the sample temperature, the energy resolution of the facility, the normalization factor and the background corrections.
- Other Model parameters (coming from theory/experiment with uncertainties) whose knowledge is necessary.
- ...

In parameter estimation techniques, these additional ingredients are called nuisance variables whose properties are not of particular interest in itself, but are fundamental for assessing reliable model parameters.

Solutions

A-priori work : treating experimental data

- re-analyse experiments from raw data with a proper systematic uncertainty description,
- simulate these uncertainties from Exfor (Conrad) :
 - to take into account a normalization uncertainty :
New data = data * N where $N = 1 \pm \delta N$,
 - to take into account a background uncertainty :
New data = data - B where $B = 0 \pm \delta B$

A-posteriori work : treating during/after adjustment

- Retro-active analysis (Conrad, Sammy) : no experiment during uncertainty analysis
- Marginalization techniques (Conrad) ; examples :
 - marginalize the normalization parameter :
New Theory = Theory/N where $N = \langle N \rangle \pm \delta N$,
 - marginalize the background parameter :
New Theory = Theory + B where $B = \langle B \rangle \pm \delta B$



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Peele's pertinent puzzle



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When ? How ?

- Appears when a full experimental covariance matrix (with systematic uncertainty) is used
- Peele noticed that the minimization of the a least square function could lead to abnormally low results.
- Observation on the ^{239}Pu capture cross section

Analysis of 1st ^{239}Pu resonance with G_{win} capture measurement⁽¹⁹⁷¹⁾

- data are used until 1 eV,
- no uncertainty in the base EXFOR,
- we chose to associate with this measure a 1% statistical uncertainty and 3% of systematic uncertainty on normalisation,
- adjusted parameters : energy, radiative and neutronic widths.

Peele's pertinent puzzle



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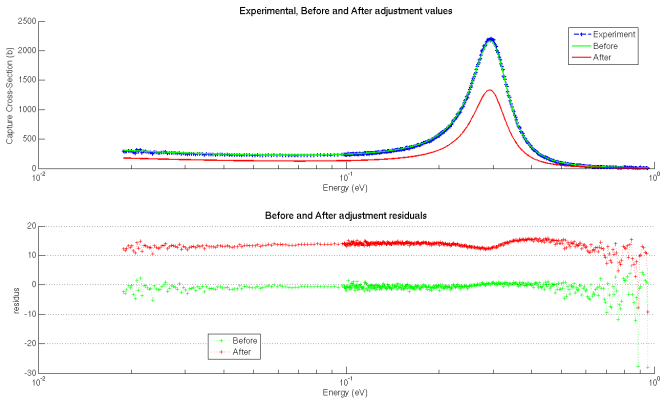


Figure: ²³⁹Pu capture cross section (before and after adjustment) and residuals.

Solution : Marginalization



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First introduced in Sammy [1, 2] :

- "retroactively" generate covariance matrix for already evaluated resonance parameters
- calculate the matrix elements knowing the theoretical cross sections, the statistical uncertainty and the nuisance parameters.

Problems :

- based only on the theoretical curves
- problem of treating "real" statistical uncertainties
- depending on specific theoretical grid.

Basics of parameter estimation with Bayes' theorem

When the analysis of a new data set \vec{y} is performed:

$$p(\vec{x}|\vec{y}, U) = \frac{p(\vec{x}|U) \cdot p(\vec{y}|\vec{x}, U)}{\int d\vec{x} \cdot p(\vec{x}|U) \cdot p(\vec{y}|\vec{x}, U)}$$

U : "background/prior" information and $p(\vec{y}|\vec{x}, U)$: likelihood

Fitting procedure : estimation of the first two moments of $p(\vec{x}|\vec{y}, U)$

Marginalization techniques

With nuisance parameters :

- evaluate the influence of $\vec{\theta}$ parameters during the estimation of \vec{x} parameters.
- Bayesian marginalization of the $\vec{\theta}$ parameters [4] :

$$p_{\vec{\theta}}(\vec{x}|\vec{y}, U) = \int d\vec{\theta} \cdot p(\vec{\theta}|U) \cdot \frac{p(\vec{x}|U) \cdot p(\vec{y}|\vec{x}, \vec{\theta}, U)}{\int d\vec{x} \cdot p(\vec{x}|U) \cdot p(\vec{y}|\vec{x}, \vec{\theta}, U)}$$

Marginalization : estimation of the first two moments of $p_{\vec{\theta}}(\vec{x}|\vec{y}, U)$

Marginalization techniques

Two methods implemented in the CONRAD code :

- Monte-Carlo : calculate first two moment of marginalized distribution [4, 3]
- Analytical

Analytical marginalization equation :

Additional hypothesis : pdf are gaussians.

$$M_x^{Marg} = \left(G^{xT} G^x \right)^{-1} G^{xT} G M_x G^T G^x \left(G^{xT} G^x \right)^{-1} {}^a$$

where G is the theoretical derivative matrix : $G = \begin{pmatrix} G^x \\ G^\theta \end{pmatrix}$

and M_X is the covariance matrix : $M_X = \begin{pmatrix} M_x & M_{x,\theta} \\ M_{\theta,x} & M_\theta \end{pmatrix}$

^a $G^{xT} G^x$ is a square matrix whose size is equal to the number of model parameters, this product can be inverted if the matrix G^x has a rank equal to the number of model parameters. In practise, $N_{exp} \geq N_{parameters}$

This formulae is to be used after the fitting procedure.



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^{155}Gd test case description

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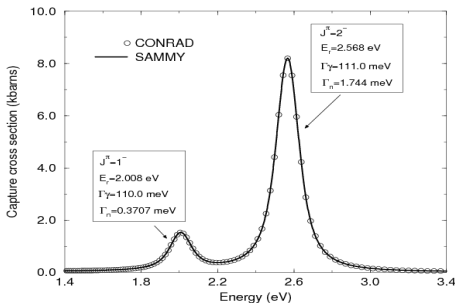
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For this work, we have selected two s -wave resonances ($E_r = 2.0$ eV and $E_r = 2.6$ eV) observed in the low energy part of the $^{155}\text{Gd}(n,\gamma)$ reaction. The analysis is restricted to a small energy range between 1.4 eV and 3.4 eV.

Virtual experiment

Comparisons of various techniques

Comparison of the uncertainties provided by the analytic and stochastic for a 3% normalization marginalization.

Resonance parameter	Analytic model (M-RLSF)		Monte-Carlo model (MC-RLSF)			
	CONRAD		CONRAD	REFIT		
Statistical unc. 1% :						
$E_R=2.0080\text{eV}$	0.000047	(0.0023%)	0.000048	(0.0024%)	0.000049	(0.0024%)
$\Gamma_\gamma=110.00\text{ meV}$	0.12	(0.11%)	0.37	(0.34%)	0.37	(0.34%)
$\Gamma_n=0.3707\text{ meV}$	0.0114	(3.07%)	0.0114	(3.07%)	0.0114	(3.07%)
$E_R=2.5680\text{ eV}$	0.000039	(0.0015%)	0.000040	(0.0016%)	0.000039	(0.0015%)
$\Gamma_\gamma=111.00\text{ meV}$	0.09	(0.08%)	0.18	(0.16%)	0.16	(0.14%)
$\Gamma_n=1.7440\text{ meV}$	0.0533	(3.06%)	0.0531	(3.05%)	0.0537	(3.08%)
Statistical unc. 5% :						
$E_R(1^-)=2.0080\text{eV}$	0.00024	(0.012%)	0.00024	(0.012%)	0.00024	(0.012%)
$\Gamma_\gamma=110.00\text{ meV}$	0.49	(0.45%)	0.60	(0.57%)	0.60	(0.54%)
$\Gamma_n=0.3707\text{ meV}$	0.0114	(3.07%)	0.0113	(3.05%)	0.0114	(3.07%)
$E_R=2.5680\text{ eV}$	0.00019	(0.0074%)	0.00019	(0.0076%)	0.00019	(0.0074%)
$\Gamma_\gamma=111.00\text{ meV}$	0.39	(0.35%)	0.43	(0.38%)	0.41	(0.34%)
$\Gamma_n=1.7440\text{ meV}$	0.0535	(3.07%)	0.053	(3.04%)	0.0539	(3.09%)
Statistical unc. 10% :						
$E_R=2.0080\text{eV}$	0.00047	(0.023%)	0.00047	(0.023%)	0.00047	(0.023%)
$\Gamma_\gamma=110.00\text{ meV}$	0.96	(0.86%)	1.02	(0.93%)	1.03	(0.94%)
$\Gamma_n=0.3707\text{ meV}$	0.0116	(3.13%)	0.0118	(3.19%)	0.0116	(3.12%)
$E_R=2.5680\text{ eV}$	0.00039	(0.015%)	0.00039	(0.015%)	0.0039	(0.015%)
$\Gamma_\gamma=111.00\text{ meV}$	0.77	(0.69%)	0.80	(0.72%)	0.77	(0.69%)
$\Gamma_n=1.7440\text{ meV}$	0.0542	(3.11%)	0.0550	(3.15%)	0.0545	(3.13%)



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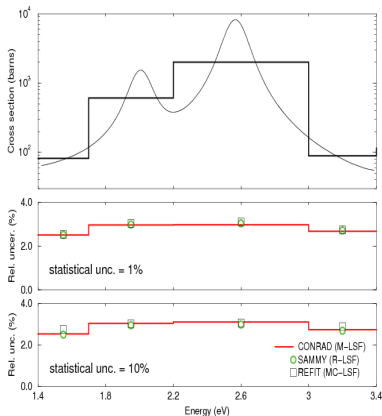
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Covariance matrices for group-average cross sections

Comparison of the point-wise and group-average ^{155}Gd capture cross section as well as retroactive results provided by CONRAD (M-RLSF), SAMMY (RLSF) and REFIT (MC-RLSF).



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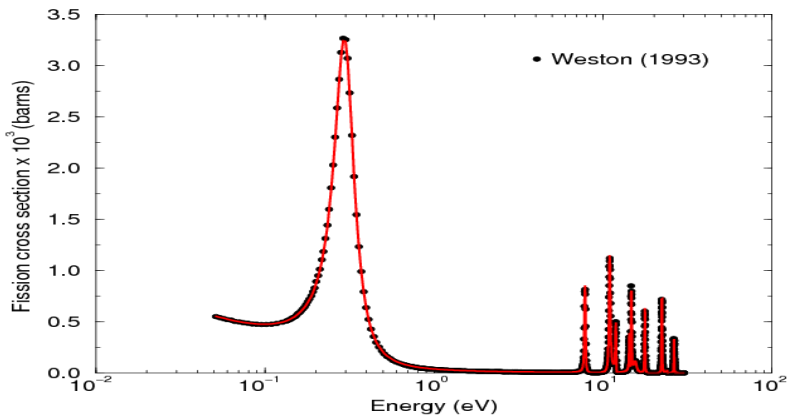
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On going work in RRR and URR

- ^{155}Gd whole resonance range
- ^{239}Pu 0eV-30eV region analysis with marginalization (capture+fission+transmission)



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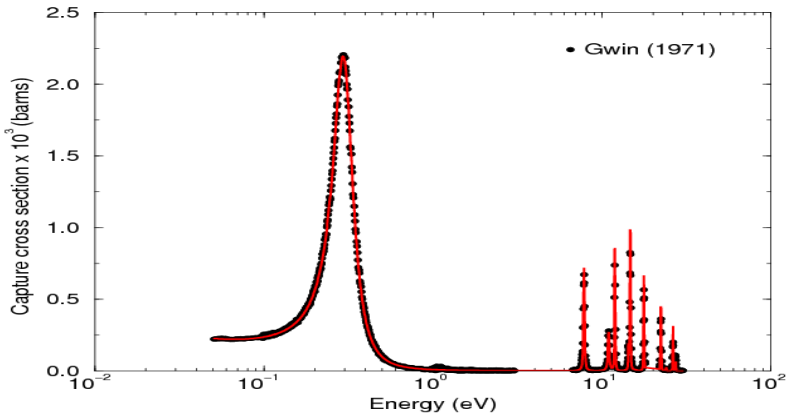
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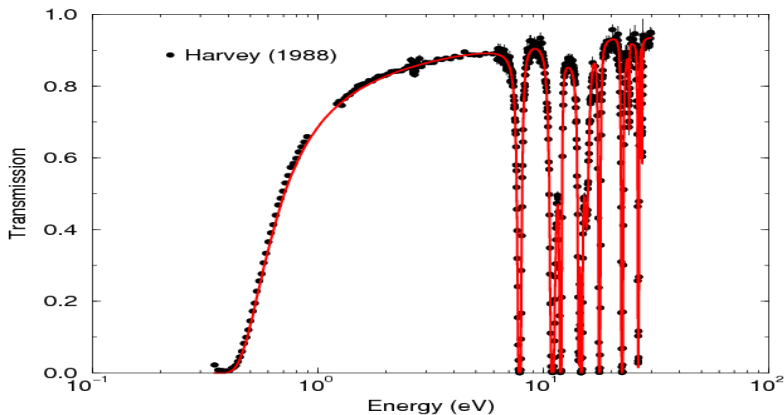
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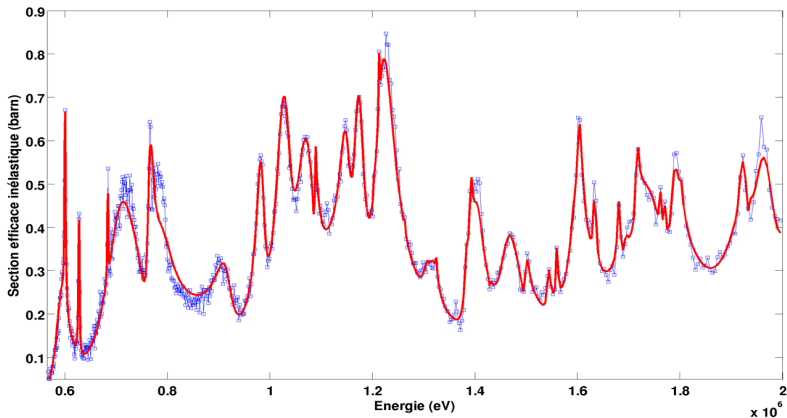
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- ^{23}Na whole resonance range + inelastique



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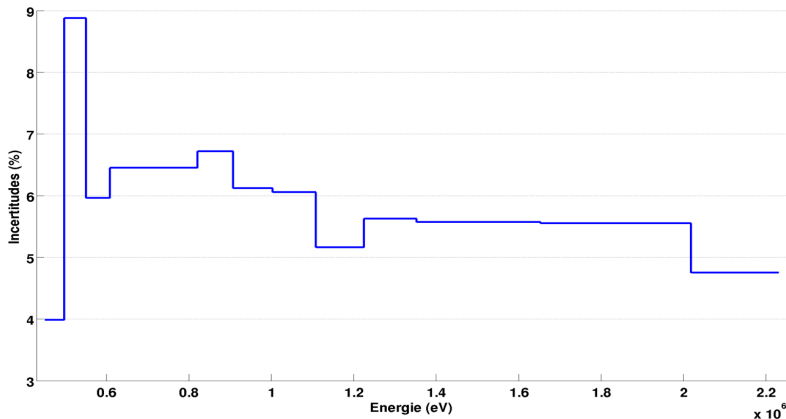
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RIPL Optical Potential : users point of view

- difficult to handle, link to physics ?
- how to define varying parameters with uncertainties ?
-a lot of zeros !!!!
- example of ^{208}Pb :

	0.001	200.0000					
	82	82					
	208	208					
	0	0	1	1	0		
	1						
	200.0000						
	1.24400	0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0
		0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0
	0.64600	0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0
		0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0
	50.60000	0.00000+0	6.90000-3	0.00000+0	1.50000-5	0.00000+0	7.00000-9
		0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0
		0.00000+0	0.00000+0	0.00000+0	0.00000+0	-5.65000+0	0.00000+0
		0.00000+0	0.00000+0	0.00000+0	0.00000+0	1.00000+0	0.00000+0
	1						
	200.0000						
	1.24400	0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0
		0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0
	0.64600	0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0
		0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0	0.00000+0
	etc					

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Conrad wrapping ECIS :

- readable, link to OMP energy dependence
- possible to define varying parameters with uncertainties
- example of ^{208}Pb :

```
[/Theory/NuclearModel]
  NuclearModelType = "ecis"
[/Theory/OpticalModel]
  OpticalModelType = "KoningDelaroche"
  EFermi = -5.65219
  Idr = 0
[/Theory/OpticalModel/RealVolume]
  r_0 = 1.244 +/- 0.0622 *CONSTANT*
  a_0 = 0.646 +/- 0.0323 *FITTED*
  p_0 = 50.6 +/- 2.53 *FITTED*
  p_2 = 0.0069 +/- 0.000345 *FITTED*
  p_4 = 1.5e-05 +/- 7.5e-07 *CONSTANT*
  p_6 = 7e-09 +/- 3.5e-10 *CONSTANT*
  p_17 = -5.65 +/- 0.2825 *CONSTANT*
[/Theory/OpticalModel/ImagVolume]
  p_0 = 15.6 +/- 0.78 *FITTED*
  p_2 = 88 +/- 4.4 *FITTED*
[/Theory/OpticalModel/ImagSurface]
  r_0 = 1.246 +/- 0.0623 *CONSTANT*
  a_0 = 0.51 +/- 0.0255 *FITTED*
  p_0 = 13.8 +/- 0.69 *FITTED*
  p_1 = 0.018 +/- 0.0009 *FITTED*
  p_5 = 13.8 +/- 0.69 *FITTED*
etc .....
```

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^{208}Pb test case description



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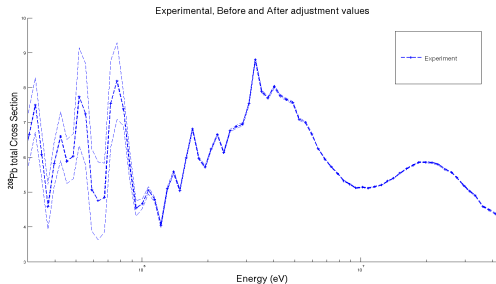
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For this work :

- Raw Datas from EXFOR

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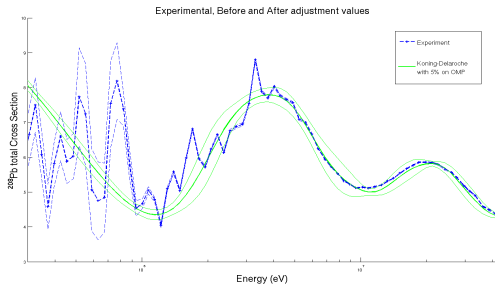
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For this work :

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- Koning-Delaroche Optical potential (with 5% uncertainty on parameter)

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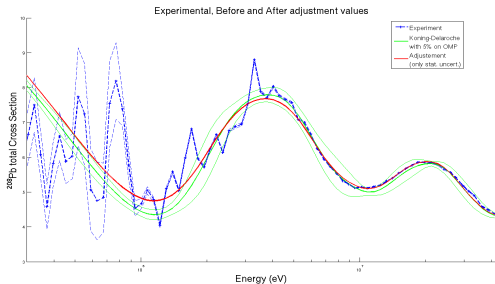
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For this work :

- Raw Datas from EXFOR
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- adjust major parameters on experiment (only stat. uncert.)

^{208}Pb test case description



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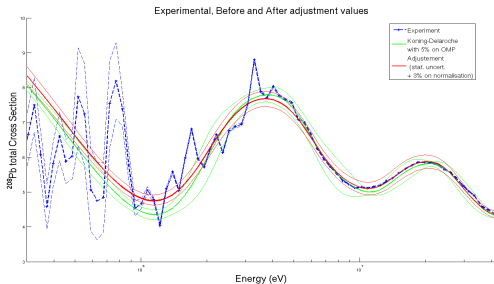
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For this work :

- Raw Datas from EXFOR
- Koning-Delarochie Optical potential (with 5% uncertainty on parameter)
- adjust major parameters on experiment (only stat. uncert.)
- adjust major parameters on experiment + marginalization of normalization (3%)



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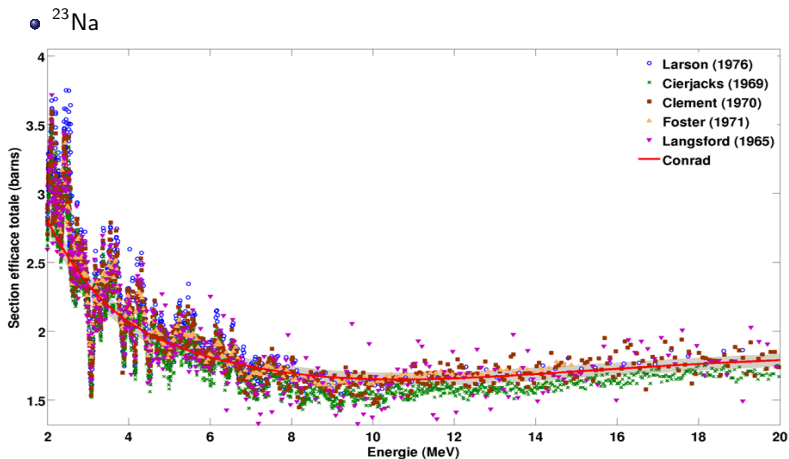
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- high energy region covariances must be evaluated

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- high energy region covariances must be evaluated
- with precautions :
 - using Optical Potential with unknown uncertainties give unresasonable and un-trusted uncertainties

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- high energy region covariances must be evaluated
- with precautions :
 - using Optical Potential with unknown uncertainties give unresasonable and un-trusted uncertainties
 - evaluate xs covariances only with experimental stat. uncert. is unphysical



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- high energy region covariances must be evaluated
- with precautions :
 - using Optical Potential with unknown uncertainties give unresasonable and un-trusted uncertainties
 - evaluate xs covariances only with experimental stat. uncert. is unphysical
 - adding experimental systematic uncertainty is obligatory



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- high energy region covariances must be evaluated
- with precautions :
 - using Optical Potential with unknown uncertainties give unresasonable and un-trusted uncertainties
 - evaluate xs covariances only with experimental stat. uncert. is unphysical
 - adding experimental systematic uncertainty is obligatory
- end-up with fairly high uncertainties (example here 3% on xs): need of additional informations



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- **Integral experiments !**

Integral experiment ?

- international benchmark ICSBEP,
- analytic experiments on reactor mock-up (EOLE, MASURCA,...)



- clean reactor irradiations (PHENIX)

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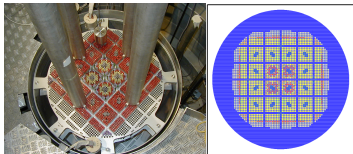
- clean reactor irradiations (PHENIX)

Not all experiments are good candidates :

- well described experiment : C/E discrepancies targeted

Integral experiment ?

- international benchmark ICSBEP,
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- clean reactor irradiations (PHENIX)

Not all experiments are good candidates :

- well described experiment : C/E discrepancies targeted
- experiment must be properly calculated :
 - bias calculated (C/C')
 - sensitivity coefficients available

Original Information from Microscopic experiments

- the analysis of microscopic experimental set \vec{y} is performed "giving" the following cost function :

$$\chi_{GLS}^2 = (\vec{x} - \vec{x}_m)^T M_x^{-1} (\vec{x} - \vec{x}_m) + (\vec{y} - \vec{t})^T M_y^{-1} (\vec{y} - \vec{t})$$

Additional Information from Integral experiments

- $\vec{y} \rightarrow \vec{E}$: vector of size $N_E = \text{Number of Integral Experiments}$
- M_E is then experimental covariance matrix
- $\vec{t} \rightarrow \vec{C}$: vector of size $N_E = \text{Number of Integral Experiments}$

\vec{E} is a set of measurements which is related to cross sections (k_{eff} , ...) and \vec{C} its associated set of calculated values (from neutronic codes, for example ERANOS, APOLLO2, TRIPOLI-4,...).

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The treatment of Integral experiments

The solution is to mix both microscopic and integral measurements in the same generalized least square :

$$\begin{aligned}\chi_{GLS}^2 &= (\vec{x} - \vec{x}_m)^T M_x^{-1} (\vec{x} - \vec{x}_m) \\ &+ (\vec{y} - \vec{t})^T M_y^{-1} (\vec{y} - \vec{t}) \\ &+ \left(\vec{E} - \vec{C}(\sigma(\vec{x})) \right)^T M_E^{-1} \left(\vec{E} - \vec{C}(\sigma(\vec{x})) \right)\end{aligned}$$

\vec{y} being the set of microscopic experiments and \vec{E} the set of integral experiments.

To implement previous equations, one has to calculate the gradient of \vec{C} with respect to the \vec{x} parameter set (nuclear reaction model parameters):

$$G(i,j) = \frac{\partial C_i}{\partial x_j}$$



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Three different methods are implemented in the CONRAD framework to calculate the derivative matrix G :

- the low fidelity method, where G will be called G_{lf} ,
- the coupled method, where G will be called G_{cc} ,
- the reference or exact method, where the derivative matrix will be denoted as G_{ref} .

The treatment of Integral experiments: reference method

Assuming that there are N_x parameters and N_E integral values, we will create $(2N_x + 1)$ evaluations from CONRAD calculations for the reference method :

- one based on the values of the parameters set \vec{x} used to calculate \vec{C} ,

Then, for each parameter x_j from \vec{x} , we will create two evaluations based :

- on the parameters vectors $\vec{x}_{+\delta x_j} = \{x_0, \dots, x_j + \delta x_j, \dots, x_{N_x}\}$
- and $\vec{x}_{-\delta x_j} = \{x_0, \dots, x_j - \delta x_j, \dots, x_{N_x}\}$.

With $\vec{x}_{+\delta x_j}$ and $\vec{x}_{-\delta x_j}$, we can calculate $\vec{C}^{+\delta x_j}$ and $\vec{C}^{-\delta x_j}$ Finally, the derivative matrix G_{ref} for the reference method is described as:

$$G_{ref}(i, j) = \frac{\partial C_i}{\partial x_j} \simeq \frac{C_i^{+\delta x_j} - C_i^{-\delta x_j}}{2\delta x_j}$$

- Major drawback : very time consuming because $(2N_x + 1) \cdot N_E$ neutronic calculations needed
- Advantages : accuracy and can be applied with both deterministic and Monte Carlo codes.
- Challenges : from nuclear reaction parameters to neutronic calculation via nuclear data treatment



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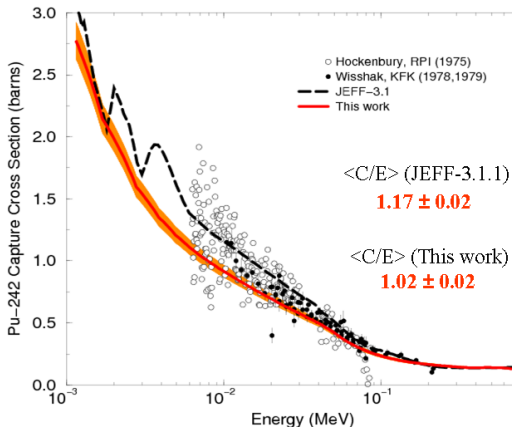
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Application to ^{242}Pu

- Profil experiments (irradiation in Phenix reactor) give highly fruitful information on capture cross section of minor actinides and several fission products.
- in several samples, $\frac{^{243}\text{Am}}{^{242}\text{Pu}}$ concentration ratio gives C/E big discrepancies

Isotopic Ratio	Sample	PROFIL C/E-1 (%)	PROFIL-2 C/E-1 (%)
$^{234}\text{U}/^{235}\text{U}$	^{235}U	-2.1 ± 1.6	0.0 ± 0.4
$^{235}\text{U}/^{238}\text{U}$	^{235}U	1.1 ± 4.8	0.0 ± 0.4
$^{236}\text{U}/^{235}\text{U}$	^{234}U		0.5 ± 0.4
	^{235}U	0.4 ± 0.2	0.4 ± 0.1
$^{239}\text{Pu}/^{238}\text{U}$	^{239}U	0.8 ± 0.8	
	^{238}U	1.1 ± 0.3	2.3 ± 0.2
$^{241}\text{Np}/^{238}\text{U}$	^{238}U		-6.7 ± 2.9
	^{238}U	0.1 ± 0.1	-2.2 ± 0.6
$^{240}\text{Pu}/^{239}\text{Pu}$	^{239}Pu	-2.1 ± 0.2	-2.3 ± 0.1
	^{239}Pu	-10.1 ± 4.1	-26.7 ± 12.6
$^{239}\text{Pu}/^{238}\text{Pu}$	^{238}U	1.9 ± 0.8	3.5 ± 0.1
	^{239}Pu	4.4 ± 1.1	3.0 ± 0.4
$^{241}\text{Pu}/^{240}\text{Pu}$	^{240}Pu	5.2 ± 0.5	3.9 ± 0.6
	^{240}Pu	16.6 ± 2.7	11.5 ± 2.9
$^{242}\text{Pu}/^{241}\text{Pu}$	^{241}Pu	9.3 ± 0.7	
	^{241}Pu	20.9 ± 1.8	14.7 ± 2.8
$^{243}\text{Am}/^{242}\text{Pu}$	^{242}Pu		-6.0 ± 1.3
$^{243}\text{Am}/^{241}\text{Am}$	^{241}Am	8.7 ± 1.9	7.6 ± 0.2
	^{241}Am	5.5 ± 1.6	10.7 ± 1.9
$^{242}\text{Pu}/^{241}\text{Am}$	^{241}Am	6.3 ± 1.5	9.7 ± 2.6
	^{241}Am	4.5 ± 1.2	
$^{242}\text{Cm}/^{241}\text{Am}$	^{242}Pu	0.0 ± 6.7	
	^{242}Pu		-2.6 ± 0.3
$^{245}\text{Cm}/^{244}\text{Cm}$	^{244}Cm		-16.4 ± 7.0
$^{233}\text{U}/^{232}\text{Th}$	^{232}Th		-8.5 ± 0.1
$^{234}\text{U}/^{233}\text{U}$	^{233}U		2.8 ± 1.9
	^{234}U		3.1 ± 0.2



Experimental systematic uncertainties :

- peele's pertinent puzzle appears with full experimental matrix
- marginalization can/must be applied in nuclear data evaluation work
- experimental conditions must be well reproduced : necessary ingredients.

Fast range covariance :

- fast range treatment is equivalent to other energy ranges (RRR) : use parameters as vector of uncertainties

Integral experiments :

- clear integral experiment can/should be used in the evaluation process
- best practises should be used and described
- interaction reactor physicists / nuclear data evaluators should :
 - append in a clear mathematical framework
 - be as far as possible automatic
 - associated with validation benchmarks to avoid non-expected discrepancies
 - needs modern tool to establish direct link between nuclear models and neutron transport codes



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